

# A statistical approach to diffusion and waiting times in the problem of melting solids

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Melting is a common phenomenon in our daily life, and although it is understood in thermodynamic terms, the transition itself has eluded a complete description from the point of view of microscopic dynamics. Our work is oriented to the study of the melting process of superheated solids, which is believed to be caused by thermal vacancies in the crystal or by the occupation of interstitial sites. When the crystal reaches a critical temperature  $T_{LS}$  above the melting point  $T_m$ , it becomes unstable and a collective self-diffusion process is triggered. These studies are often observed in a microcanonical environment, revealing long-range correlations due to collective effects, and from theoretical models using random walks over periodic lattices. Our results suggest that the cooperative motion made possible by the presence of vacancy-interstitial pairs (Frenkel pairs) [1] above the melting temperature induces long-range effective interatomic forces even beyond the neighboring fourth layer [2]. From microcanonical simulations it is also known that an ideal crystal needs a random waiting time until the solid phase collapses. Our results also point towards a description of these waiting times using a model in which there is a positive, unspecified quantity  $X$  that accumulates from zero in incremental steps, until  $X$  exceeds a threshold value  $X^*$  that triggers collapse [3]. The work proposal contemplates to incorporate the results obtained previously and study of the diffusion properties in the critical superheated phase, in particular the development of microscopic models to explain the anomalous diffusion (superdiffusion) observed in this phase [4] and studying the formalism known like continuous time random walk.

## References

- [1] X.-M. Bai and M. Li. Phys. Rev. B, 77, 134109 (2008).
- [2] V. Olgún-Arias, S. Davis, G. Gutiérrez. J. Chem. Phys., 151, 064507 (2019).
- [3] V. Olgún-Arias, S. Davis, G. Gutiérrez. Phys. A, 561, 125198 (2021).
- [4] S. Davis, A. B. Belonoshko, B. Johansson, A. Rosengren. Phys. Rev. B, 84, 064102, (2011).