

# Irregularity of polymer domain boundaries in two dimensional polymer solution

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Domain boundaries of polymer chains comprising a polymer solution confined in strict two dimensions (2D) are irregular, and their fractal dimension ( $D_p$ ) varies with the area fraction of the solution and the solvent quality. For polymers in  $\theta$  solvents,  $D_p$  remains constant at  $D_p=4/3$  from dilute to semi-dilute phase, but decreases to  $D_p=5/4$  in dense phase. In contrast,  $D_p$  in good solvents changes non-monotonically from  $D_p=4/3$  in dilute phase to  $D_p=5/4$  in dense phase, maximizing to  $D_p \approx 3/2$  at a critical area fraction. Using polymer physics arguments, we rationalize the values of  $D_p$  at some limiting conditions. We also put our discussion into the perspective of the Schramm-Loewner evolution (SLE). We find that the maximal irregularity of  $D_p \approx 3/2$  results from "fjord"-like corrugations formed in domain boundary which also maximize at the critical area fraction. In fact, 2D random curves with  $D_p=3/2$  correspond to the SLE $_{\kappa}$  with  $\kappa=4$ , which lies at a marginal point, transitioning from simple non-intersecting curves to those with self-intersections.